A User-Focused Assessment of Annual Load Estimation Methods in Small Watersheds

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***Nicholas J Gubbins****, Weston M Slaughter, Mike Vlah, Spencer Rhea, Matthew RV Ross, Emily S Bernhardt*

# Abstract

# Rivers export dissolved materials and eroded sediments from the watersheds they drain. Much can be learned about rivers and their watersheds by measuring the magnitude, timing and form of element exports. Such watershed load datasets are used to gain fundamental understanding of watershed ecosystems as well as to assess water quality and the efficacy of management approaches to sustain both terrestrial and aquatic ecosystem health. Despite the widespread use of watershed load estimates, comparisons at macrosystem-scales (e.g. across many sites) are currently complicated by differences in underlying data quality and estimation methods between sites, periods, and solutes. Using high-frequency sensor data from the Hubbard Brook Experimental Forest, we generated time series of increasingly coarse sampling frequencies, and tested the sensitivity of various load estimation methods. We further tested the accuracy of common methods using synthetic time series, spanning a range of flow regimes and concentration-discharge (C:Q) relationships. Lastly, we applied each estimation method to the MacroSheds dataset (macrosheds.org), generating a publicly available dataset of 16,489 site-years of data across 93 sites and 112 solutes. Results from both the simulated data coarsening and synthetic time series experiments indicate that load estimates with high sampling frequency (daily or better) and an informative C:Q relationship are well suited for macroscale science efforts (errors within ~10%). Estimates based on coarse (biweekly or coarser) underlying data and incomplete C:Q relationships showed large enough error (>50%) to suggest they would be misleading if included in macroscale efforts. Our results suggest that scientists interested in comparing load estimates should first consider (1)  sensitivity of their analysis to changes in load magnitudes, (2) the underlying data frequency used to generate estimates, (3) the C:Q relationship of their solute of interest, and (4) their confidence in the completeness of that C:Q relationship over the period.

# Introduction

Annual stream load is the mass of solutes or sediments that move past a point in a stream during a water year. Estimates of solute loads are a foundational measure of critical watershed-ecosystem functions–such as a watershed’s capacity to retain nutrients and potential to weather bedrock–and are valuable across disciplines. Quantifying how and when solutes move out of watershed-ecosystems gives researchers key insights into how a watershed functions as a system. In small watersheds with watertight bedrock, researchers know that water can only leave the watershed through transpiration or stream discharge (Bormann et al, 1968). If this assumption is met, researchers interested in how nutrients move through ecosystems can measure nutrient inputs from the atmosphere and soil and then measure the outputs of these nutrients in streamflow. Assessing the difference between inputs to and outputs from a small watershed can be used to estimate critical ecosystem functions such as nutrient retention, precisely and accurately (Bormann et al, 1968). However, this kind of chemical accounting relies on accurate estimates of inputs and outputs. For instance, researchers interested in nutrient dynamics rely on estimates of solute export to compare watershed functions in paired catchment studies (such as Bormann et al, 1968; Likens et al, 1970; Likens et al, 2006). Geochemists use load estimates to constrain in-watershed weathering rates (Gaillardet et al, 1999; Maher and Chamberlain, 2104). Land managers and government decision makers rely on accurate estimation of solute loads to write and apply policy (USEPA, 2000; Schilling et al, 2017).

Theoretically perfect solute loads are calculated as the product of the solute’s concentration and streamflow, integrated *continuously* over time, as shown in equation 1. Where is the load, the concentration, the streamflow, and the time.

Unfortunately, environmental data is rarely truly continuous. However, after a century of collective effort, streamflow gauging and modelling can generate reliable, near-continuous estimates of discharge for most systems of interest. To perfectly estimate flux we would need not only near-continuous discharge estimates, but also near-continuous measurements of solutes. Yet this kind of data, whether directly measured or modelled, is rare due to the labor and time involved in producing the measurements (Kirchner et al, 2004; Pellerin et al, 2014; Zimmer et al, 2019). Up until recently (Halliday et al, 2012), measuring most solutes requires a water sample to be taken to a laboratory. As a result, chemistry samples have traditionally been taken as discrete bottle samples that must be manually collected and analyzed (Kirchner et al, 2004; Pellerin et al, 2014). Sampling frequencies, therefore, have been on the order of weekly or monthly for many watershed-ecosystem studies for more than 50 years (Buso et al, 2000).

Estimating solute loads for studies with infrequent chemical sampling requires the use of models to estimate concentrations between measurements (Kirchner et al, 2004; Pellerin et al, 2014). This introduces uncertainty into truly continuous estimates of load (Richards and Holloway, 1987; Schilling et al, 2017). In recent decades, the technology to monitor water chemistry via high-frequency environmental sensors has become cost-effective enough - for a limited range of solutes - to be measured at the same frequencies as discharge is modeled (Kirchner et al, 2004; Pellerin et al, 2014). However, for researchers interested in pre-sensor time series or solutes that can’t yet be measured using continuous approaches, there is no ideal way to assess the accuracy and potential bias of load estimates (Richards and Holloway, 1986; Appling et al, 2015; Aulenbach et al, 2016).

Moreover, many different methods have been used to compute these estimates (figure 1), ranging from simple averaging or step functions (Likens et al, 1977) to complex statistical models (Appling et al, 2015; Zhang and Hirsch, 2019). Conflicting estimation methods further challenge confidence in comparing load estimates across sites­ (Appling et al, 2015; Nava et al, 2019).

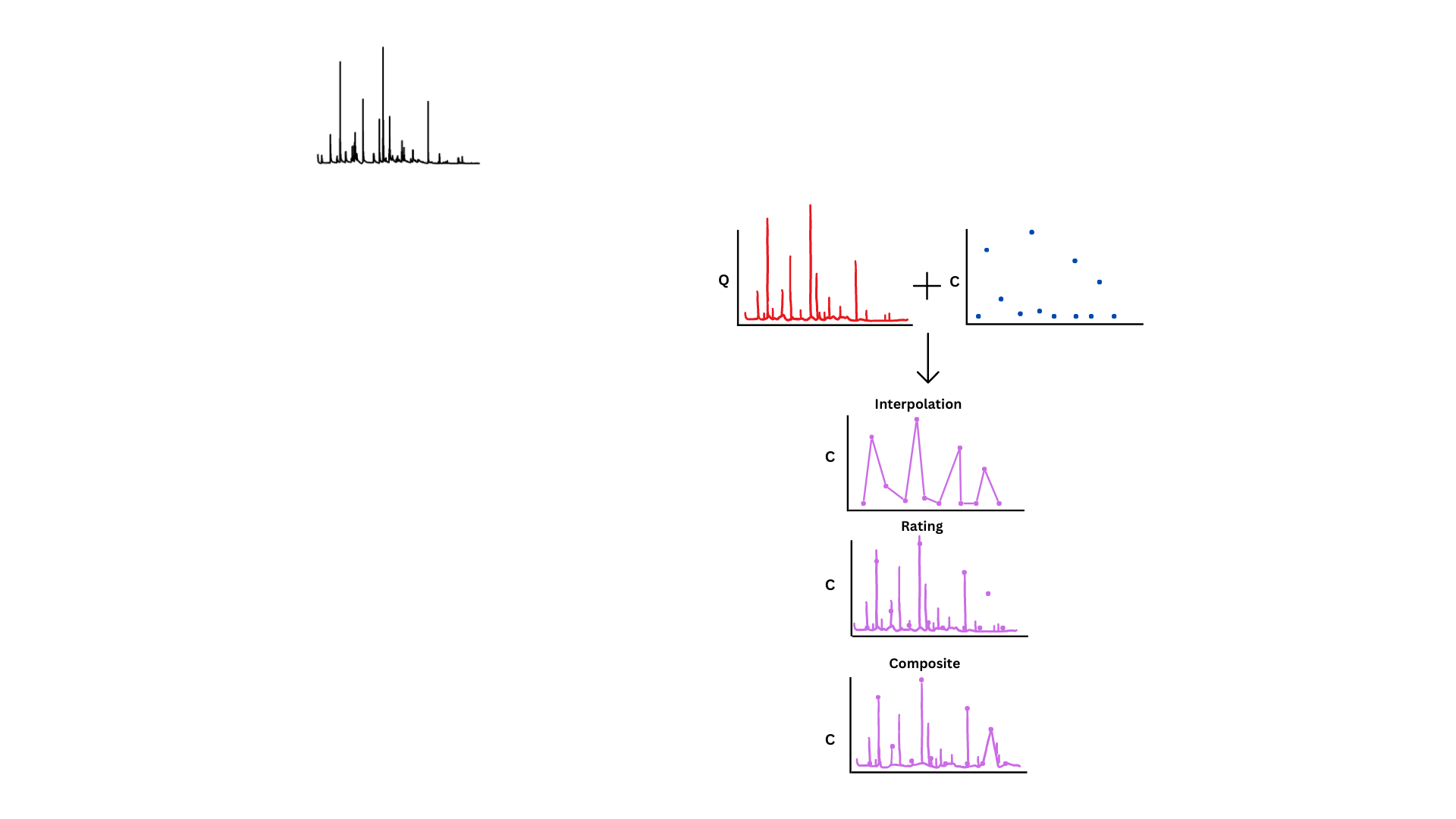


Figure 1: An illustration of concentration estimation techniques (in purple) resulting from high-frequency discharge data (in red) and intermittent, discrete chemistry samples (in blue).The Beale ratio estimator (not shown) instead applies a correction factor after generating an estimate with available data.

While some methods are more appropriate than others for a given system and solute, it is impossible to know with confidence what was missed in years sampled infrequently in the past compared to those sampled near-continuously in the present (Richards and Holloway, 1986; Appling et al, 2015; Nava et al, 2019). This puts water researchers, especially those interested in macroscale, cross-site comparisons, in a quandary, leading to the core question of this paper:

**How do we make accurate and analysis-ready load estimates that can be compared across diverse watersheds, sampling regimes, and data density?**

The challenges outlined above are only exacerbated when expanding scope from a single site and solute to many of each, where methodologies and sampling frequency can vary substantially. Thus, answering our primary research question becomes especially important for macrosystem scientists (researchers interested in working across many systems), as they are often unable to rely on the intimate, working site knowledge that can inform single site analyses. While the fundamental problems presented here cannot necessarily be solved - many recent, parallel efforts have aggregated and unlocked previously scattered, complicated, and challenging data. For example, the CAMELS dataset has complied high quality hydrology, basin, and climate data for well-sampled USGS sites into a single database (Newman et al, 2014). The work the CAMELS team has done to harmonize and document these data has significantly lightened the repetitive, pre-analysis burden that macrosystem scientists face. Ultimately allowing these researchers to spend proportionally more time and resources on advancing continental science.

Many efforts have been taken to improve the accuracy of solute load estimates and provide recommendations for approaches (Richards and Holloway, 1986; Appling et al 2015; Aulenbach et al, 2016; Shilling et al, 2017; etc.), but those efforts have either focused on large watersheds (Pellerin et al, 2014, Appling et al, 2016; Schilling et al, 2017) or on choosing the best method possible for a given time series (Richards and Holloway, 1986; Aulenbach et al, 2016). While both areas of research are deeply important for the field at large, they do not clearly delineate when load estimates can be used in cross-site comparisons. This study seeks to build on these prior efforts with three goals. (1) To provide clear guidance to macroscale scientists on what degree of confidence to have in load estimates originating from small watershed studies, (2) to provide flux estimates for a synthesis dataset of small watershed studies and, (3) provide a framework for classifying potentially comparable flux estimates for cross-site analyses.

# Methods

To understand how and when we can make comparable load estimates between sites we need to understand:

1. How sensitive are commonly used estimation methods to varying frequencies of concentration sampling?

2. How does this sensitivity scale with the variance and drivers of the concentrations sampled?

3. Can we reliably choose the best available estimation method using only solute concentration and discharge data?

To tackle the first question, our study uses a case study of data from the Hubbard Brook Experimental Forest (HBEF) to show the relative effect of estimation method and sampling frequency on load estimation error for two solutes. We then apply our case study methods on synthetic time series data to explore the second question across a range of hydrologic regimes and solute chemodyamics. To explore question three, we test a simplified application of a published decision tree for method selection. Lastly, we apply our tested methods to the geographically diverse Macrosheds synthesis dataset (Vlah et al, 2023), providing a dataset to be used for future investigations.

## Load Estimation

Four common load methods were chosen for this study: linear interpolation (LI), Beale ratio, rating, and composite. These methods were chosen as they are archetypical of the array methods commonly used in small watershed ecosystem studies. Previous work has shown that methods should be matched to the chemodynamics and data density of the time series of interest (Aulenbach et al, 2016).

### Linear Interpolation

Linear interpolation (figure 1, top left) is performed by linearly interpolating sampled chemistry values to match their accompanying discharge time series, then computing loads by summing the time series, as represented in equation 2.

Where is the load in kg/ha/year, is the interpolated concentration in mg/L, and is the streamflow in Lps. Due to its simplicity, linear interpolation is commonly used in studies, especially where load estimation methods are not the focus. The method has been shown to work well for frequently sampled time series (Appling et al, 2015) and in time series where concentrations are highly autocorrelated (Aulenbauch et al, 2016). For example, this approach has been used to estimate fluxes of nutrients and suspended sediments in the Santa Ynez Mountains (Coombs and Melack, 2012) and in describing solute export from catchments in the Bonanza Creek LTER study site (Petrone eta al, 2006). We used the ‘RiverLoad’ R package’s ‘method6’ function to apply linear interpolation (Nava et al, 2019).

### Beale Ratio Estimator

The Beale ratio estimator (figure 1, top right) is often chosen for use in studies for its ability to provide unbiased results (Meals et al, 2013; Nava et al, 2019). This method first calculates a mean daily load with a product of concentration and discharge for days with data for both parameters. Then, a ratio of total flows sampled for chemistry over total flows observed and information on how and covary is used to scale the resulting load estimate, as represented in equation 3.

Where is the mean flow for when concentration was measured and is the mean of flow for the entire year. We used the ‘RiverLoad’ R package’s ‘beale.ratio’ function to apply the Beale ratio estimator, which relies on the Beale ratio as described in Beale 1962. This approach is often used by the US Environmental Protection Agency (EPA) in estimating loads (Meals et al, 2013). Current use of the Beale ratio estimator is often improved by the EPA’s AutoBeale tool.

### Rating

The rating method (figure 1, bottom left) first relates concentration to discharge in log-log space with a simple linear model. Then the resulting least square regression line is used to generate a full time series of concentrations using the discharge time series as an input. Values are then summed for the year to generate load, just as in linear interpolation. This method has been shown to be very effective when the solute of interest has a strong concentration-discharge relationship (Crawford, 1999; Quilbe et al, 2006). We used the ‘RiverLoad’ R package’s ‘rating’ function to generate rating estimates. The simple application of this method has been used to estimate nutrient loading in the Illinois River (Vieux and Moreda, 2003). Generally, current efforts tend to favor more sophisticated regression methods, such as the USGS’s Weighted Regressions on Time, Discharge, and Season (WRTDS) tool.

### Composite

The composite method (figure 1, bottom right) follows the same steps as the rating method, but the resulting daily concentration time series is corrected back to the observed values used to generate the rating. First, a rating is fit as described in the previous section. Then, residuals between each observation and the rating derived concentration at that time are calculated. The residuals are then applied as a correction to the derived time series at each sampled point. Each residual correction is then linearly interpolated between sampled days to generate a final time series. In essence, the rating generated time series is ‘forced through’ all known observations. This time series is then summed to compute annual loads. The composite method has been shown to combine the strengths of linear interpolation and the rating method (Aulenbach and Hooper, 2006; Appling et al, 2015; Aulenbach et al, 2016). Our application of the composite method was adapted from Appling et al 2015. The composite method has become a primer choice for many loading analyses. For example, it has been used to calculate nutrient export in urban streams in Puerto Rico (McDowell et al, 2018), to estimate sulfate export at Niwot Ridge LTER site in Colorado (Crawford, 2019), and is often favored by the US Geological Survey (Zhang and Hirsch, 2019).

## Comparing Subsampled Data to High Frequency Data

To estimate each method’s sensitivity to solute and sampling frequency, we performed a data coarsening experiment on two time series from the watershed 3 site at HBEF, one of nitrate as nitrogen (NO3 – N) and one of calcium (Ca) (figure 2).

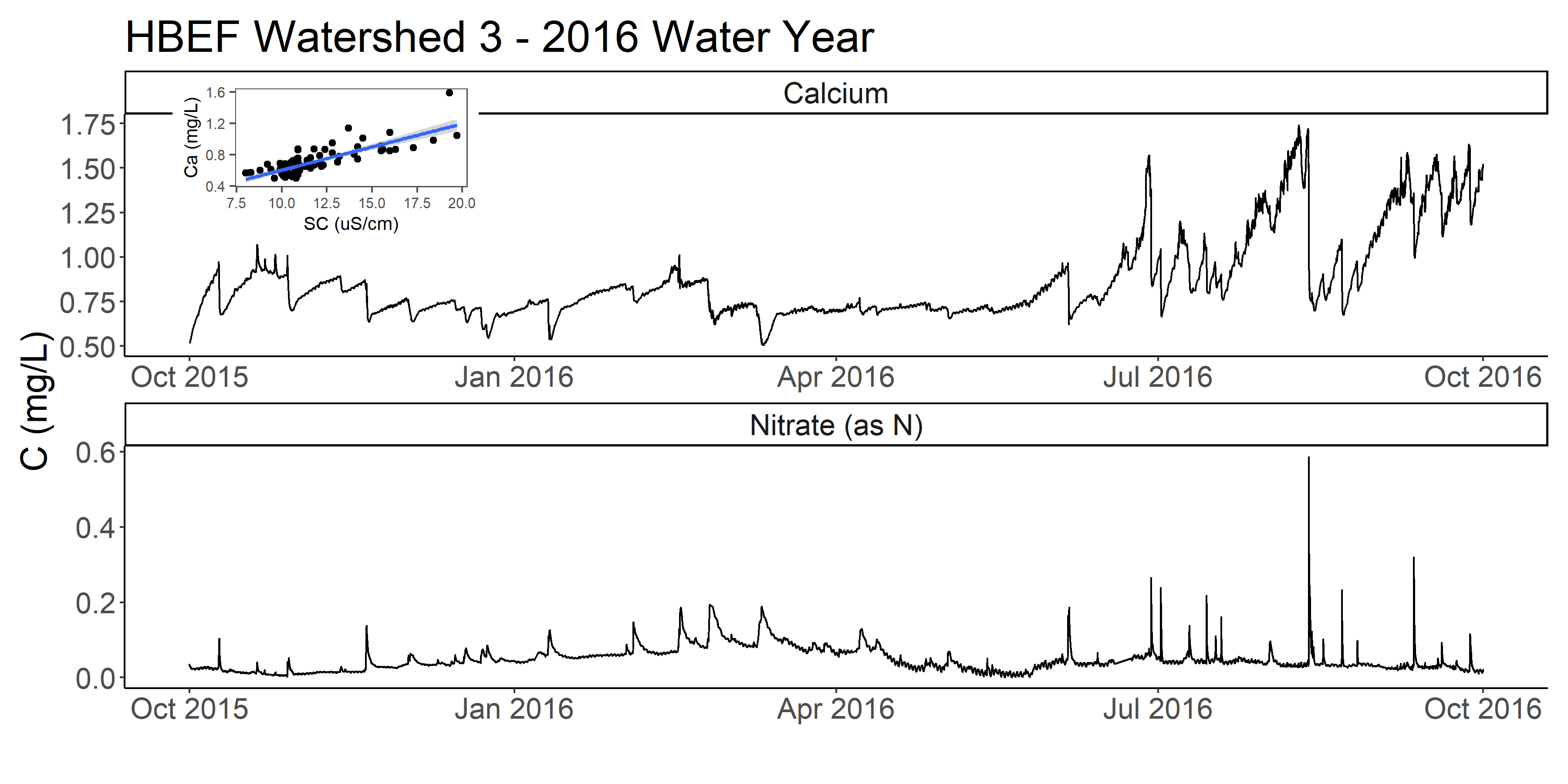


Figure 2: The underlying chemistry time series used in the data coarsening experiments. Data was collected at Hubbard Brook Experimental Forest in watershed 3 using a multiparameter sonde.The NO3-N time series was measured by the sonde directly. The Ca time series was derived from measurements of specific conductance regressed against grab samples of calicum. The record has no missing days.

Both time series were collected over the 2016 water year at a 15-minute frequency using a multiparameter sonde in conjunction with a longrunning stream gauge. The Ca time series was constructed by fitting a least square regression line with no intercept between specific conductance sensor readings and Ca grab samples taken at the site (Figure 2, inset). The NO3 – N time series had a mean concentration of 0.048 mg/L with a standard deviation of 0.032 mg/L. The Ca time series had a mean concentration of 0.86 mg/L with a standard deviation of 0.23 mg/L. The Ca time series was complete for the year, with no missing days. The NO3 – N time series had 3 days with incomplete data (2/25/2016, 6/18/2016, and 6/23/2016) and 4 days with no data (6/19/2016-6/22/2016).

The discharge time series (figure 3) is complete, with a mean flow of 8.94 Lps, a flow standard deviation of 19.20 Lps, and a yield of 2.6 x 1010 liters for the year. The steep dip between 1/2/2016 and 1/10/2016 was caused by freezing at the site. Hydrologists at HBEF use the robust ensemble method for imputing streamflow during freezes by using data from nearby, non-frozen gauges, as described in See et al 2020.

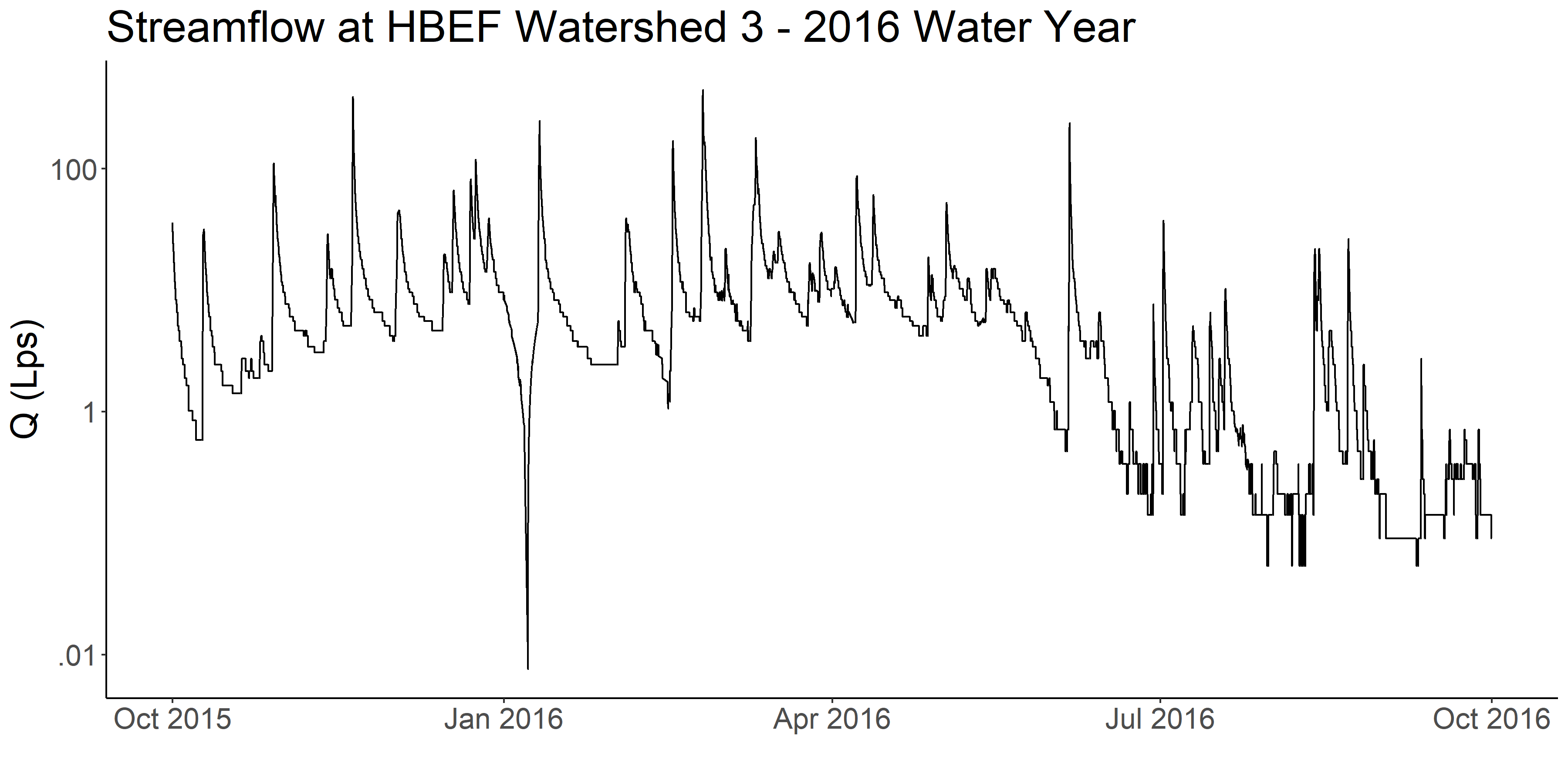


Figure 3: The underlying streamflow data used in the data coarsening and synthetic time series experiments. Data was collected at Hubbard Brook Experimental Forest in watershed 3 using a long-running rating, v-notch weir, and stage recorder.

The underlying concentration-discharge relationships for both solutes over the year are presented in figure 4.

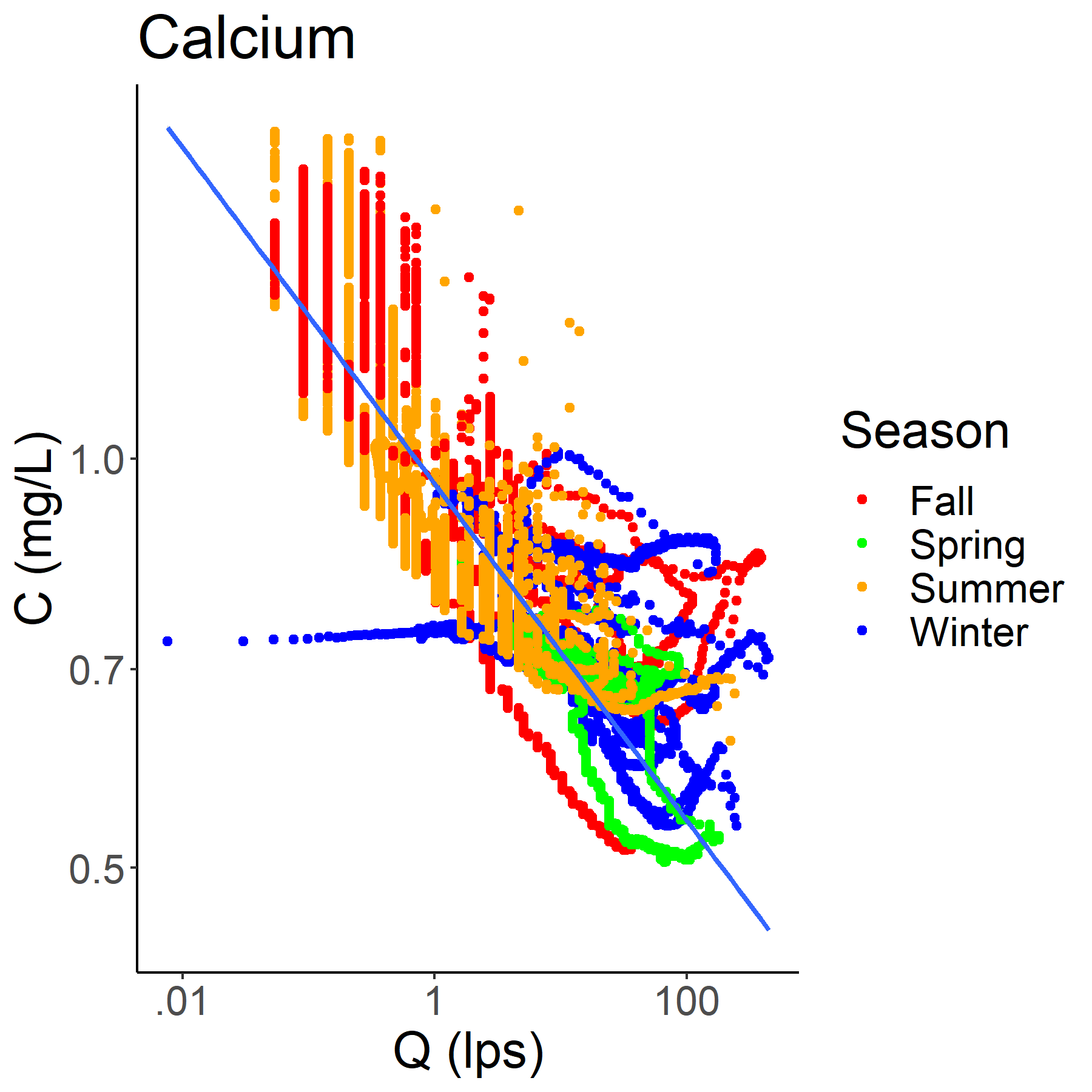
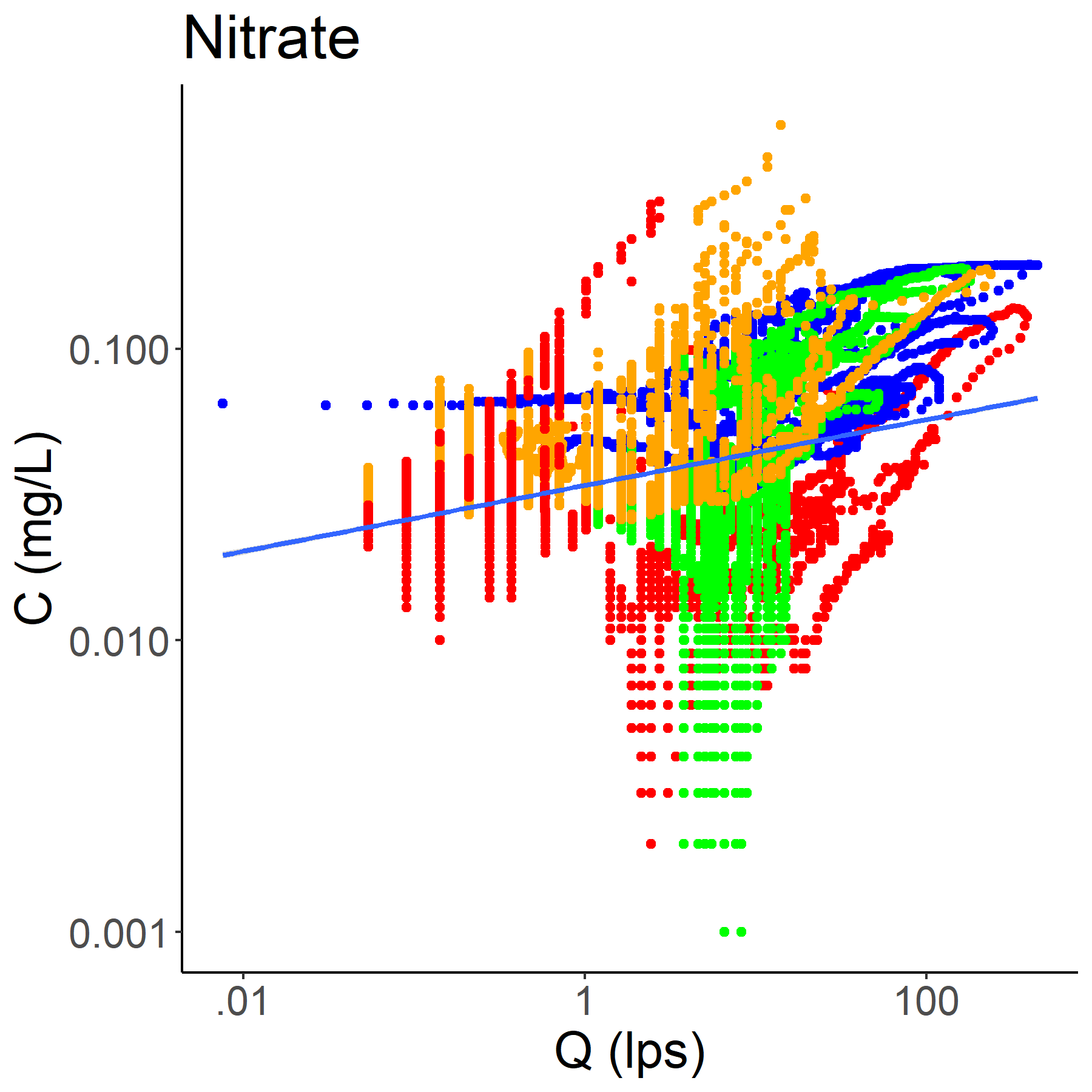


Figure 4: Concentration-discharge plot for NO3-N and Ca at HBEF watershed 3 for the 2016 water year. Observations are in black and the least squares regression line used in the rating and composite methods is in blue. Note the presence of hysteresis loops and seasonality that our methods do not handle. The slope of the best fit line is 0.11 with an r-squared of 0.07 for NO3-N and -0.12 with an r-squared of 0.79 for Ca. The NO3-N time series has a mean of 0.048 mg/L and a standard deviation of 0.032 mg/L. The Ca time series has a mean of 0.86 mg/L and a standard deviation of 0.22 mg/L.

There is a very weak relationship between NO3-N and discharge, with a log-log least square regression slope of 0.11 and r-squared of 0.07. In contrast, Ca showed a strong, diluting concentration-discharge relationship, with a log-log least square regression slope of -0.12 and r-squared of 0.79.

### Coarsening Procedure

We coarsened each time series from the full, 15-minute resolution to daily by hour (sampled hourly, every other hour, every third hour, …, every 24th hour), from daily to weekly by day (sampled every day, every other day, every third day, …, every seventh day), and then to monthly and bimonthly discretely, as partially illustrated in figure 5.

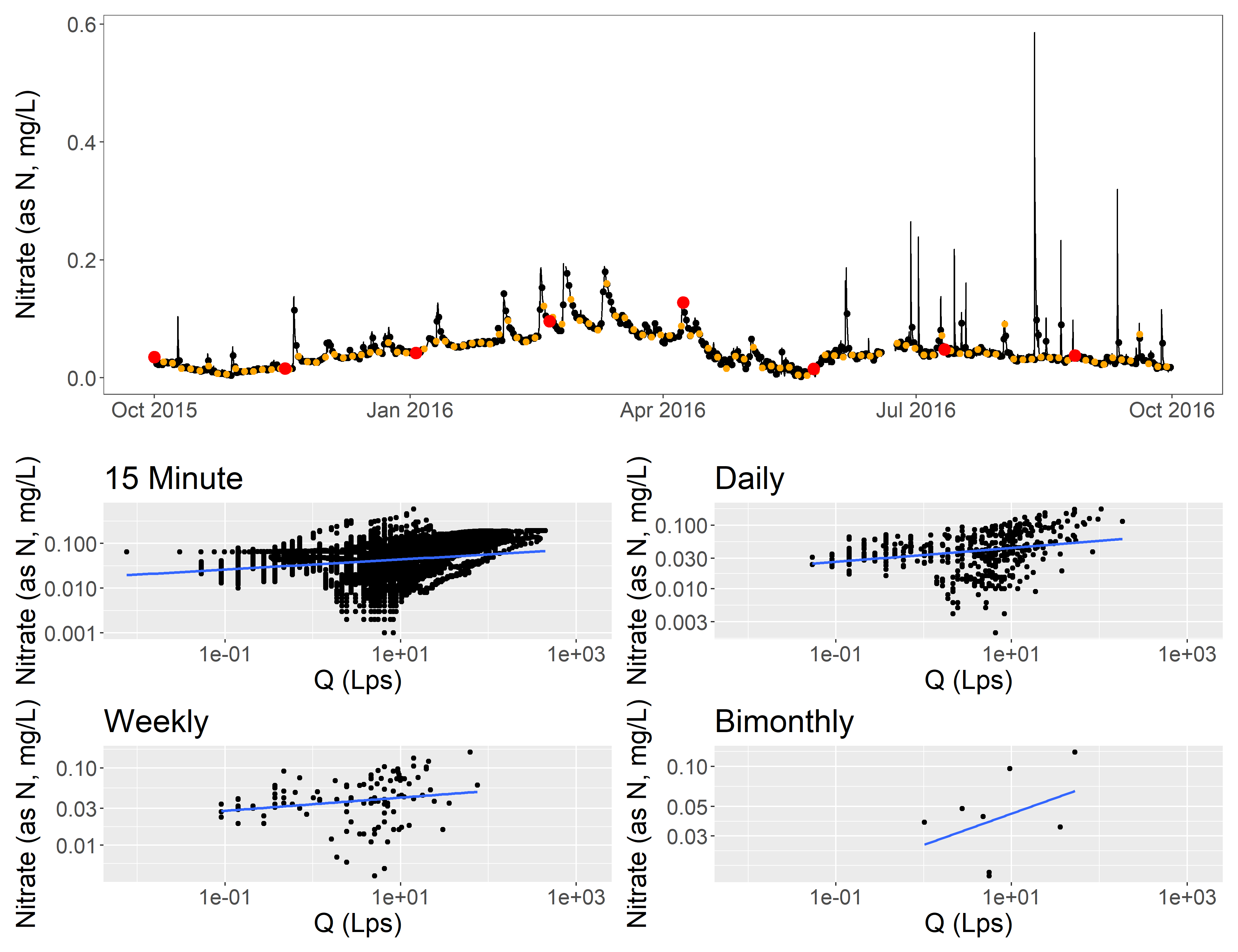


Figure 5: A selection of gradually coarsened nitrate time series generated from the original, 15-minute Hubbard Brook sensor time series (black line). Coarsened daily (black points), weekly (orange points), and bimonthly (large, red points) are shown as an example. The resulting concentration-discharge relationships are shown below. This process was repeated with a random starting position 100 times to create a range of possible time series from the original data.

A random starting point from within each initial coarsening interval was chosen and then every nth sample was then taken to create a coarsened time series. We then applied each method to each coarsened time series and the full discharge record to generate annual flux estimates. This process was repeated 100 times to generate an envelope of possible estimates with each method.

### Calculating and Comparing to ‘True’ Load

‘True’ load was calculated by applying the composite method to the full, high frequency time series (as recommended in Aulenbach et al 2016). We then calculated percent error by comparing true load and estimates generated with the coarsened time series.

## Comparing model efficacy for synthetic datasets with varying C\*Q relationships

Due to the limited availability of high-quality, high-frequency senor and streamflow data from small watersheds, we created synthetic time series to test the sensitives of each method to various hydrologic and concentration-discharge relationships.

Past work has shown that the best available load estimation method depends largely on the autocorrelation of chemistry samples through time - driven either by sampling frequency or in situ processes - and the relationship between solute concentration and discharge (Aulenbach et al, 2016). The variance (including diurnal, seasonal, and interannual) and concentration-discharge relationship of a given solute over time define its chemodynamics. Solutes with high variance and/or with strong concentration-discharge relationships are considered chemodynamic (Godsey et al, 2009; Koger et al, 2018; Godsey et al, 2019). Non-variable, non-discharge related solutes are considered chemostatic (Godsey et al, 2009; Koger et al, 2018; Godsey et al, 2019). Chemodynamism has been observed in many forms. Some commonly chemodynamic solutes, like dissolved organic matter, often increase with increasing discharge, or are called enriching (Moatar et al, 2017). The opposite is true of many geochemical solutes, such as magnesium or potassium. Instead, they often dilute as flows increase (Moatar et al, 2017; Godsey et al, 2009). Additionally, solutes can display complex chemodynamics that change as flows increase (Moatar et al, 2017). Solutes can also display no pattern with streamflow, but vary widely due to other factors, such as environmental biotic demand. This is often true of nutrients, such as nitrate (Pellerin et al, 2014; Schilling et al, 2017). Given the underlying assumptions used in the estimation methods outlined above, understanding the underlying chemodynamics of a given solute is critical to selecting an appropriate method (Appling et al, 2015; Aulenbach et al, 2016).

Using the discharge record from HBEF watershed 3 in the 2016 water year as a starting point, we created batches of three idealized hydrologic regimes and four idealized concentration-discharge relationships to test our flux methods. We have grounded our analysis in known methods where possible and the code used to create the data is publicly available at FINAL GITHUB LINK.

### Hydrologic Regimes

We fit an autoregressive integrated moving average (ARIMA) model to the flow record used in the data coarsening experiments using the ‘forecast’ R package’s ‘auto.arima’ function (Khandakar, 2008). Then, residuals from the model were randomly reshuffled and applied to the original time series, as described in equation 4.

Where is the resulting for the day, is the observed discharge at that time, is the randomly reshuffled residual for that day, *k* is a constant to prevent zero flow days, and the ratio term is a hold-factor which adjusts the total water yield each generated year the water year of the input time series.

The same modeling method was then applied to generate stormflow dominated and baseflow dominated time series, as described in equations 5 and 6 respectively.

Where the exponent applied to attenuates the flow, creating a larger or smaller stormflow signal. The baseflow time series was then attenuated with a moving average to reduce noise using the ‘zoo’ R package’s ‘rollmean’ function with a *k* value of 10 (Zeileis and Grothendieck, 2005).

We repeated this process 100 times to create a range of potential site-years under each hydrologic regime. An example of a single run is illustrated in figure 6.

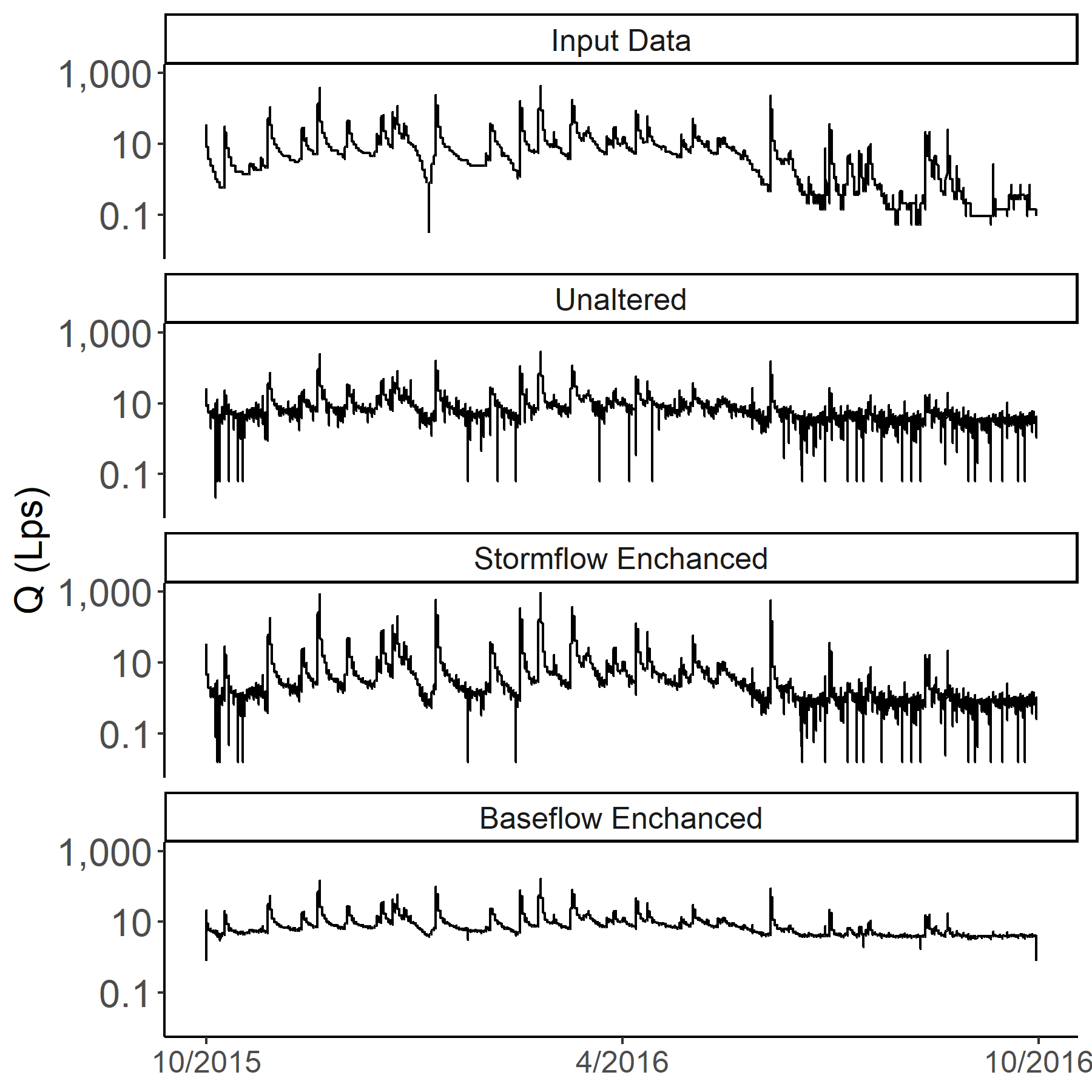


Figure 6: Examples of the hydrology time series created for this study. The raw, input data (top) was used to fit an ARIMA model. The residuals of this model fit were then randomly reshuffled to create the three modeled time series. This process was repeated 100 times. The unaltered time series only has reshuffled residuals. The stormflow enhanced series has been transformed to have a ~15% increase in quickflow. The baseflow enhanced time series had a ~15% reduction in quickflow. Note that each time series has the same total flux of water, only the timing of the delivery changes.

We used the ‘EcoHydRology’ R package’s ‘BaseflowSeperation’ function to determine proportion of quickflow to total flow for each time series (Fuka et al, 2014). The unaltered time series had ~20% quickflow, the stormflow time series had ~35% quickflow, and the baseflow time series had ~5% quickflow.

### Concentration-Discharge Regimes

To generate chemostatic time series of stream chemistry, we randomly sampled a normal distribution of points with a mean of 2 mg/L and a standard deviation of 0.1 mg/L for each day in the generated streamflow timeseries. Likewise, to generate our no-pattern time series we randomly sampled a normal distribution of points with a mean of 2 mg/L and a standard deviation of 0.5 mg/L for each day in the generated streamflow timeseries.

To generate time series of enriching stream chemistry, we applied equation 7 to our generated streamflow time series.

Similarly, we applied equation 8 to generate time series with diluting chemistry.

We then added error to the enriching and diluting time series by taking the product of each and an error factor, randomly drawn for each day from a normal distribution with a mean of 1 and a standard deviation of 0.1.

We applied each of these methods to each hydrology time series generated in the previous section. An example of the resulting concentration-discharge relationships formed are illustrated in figure 7.

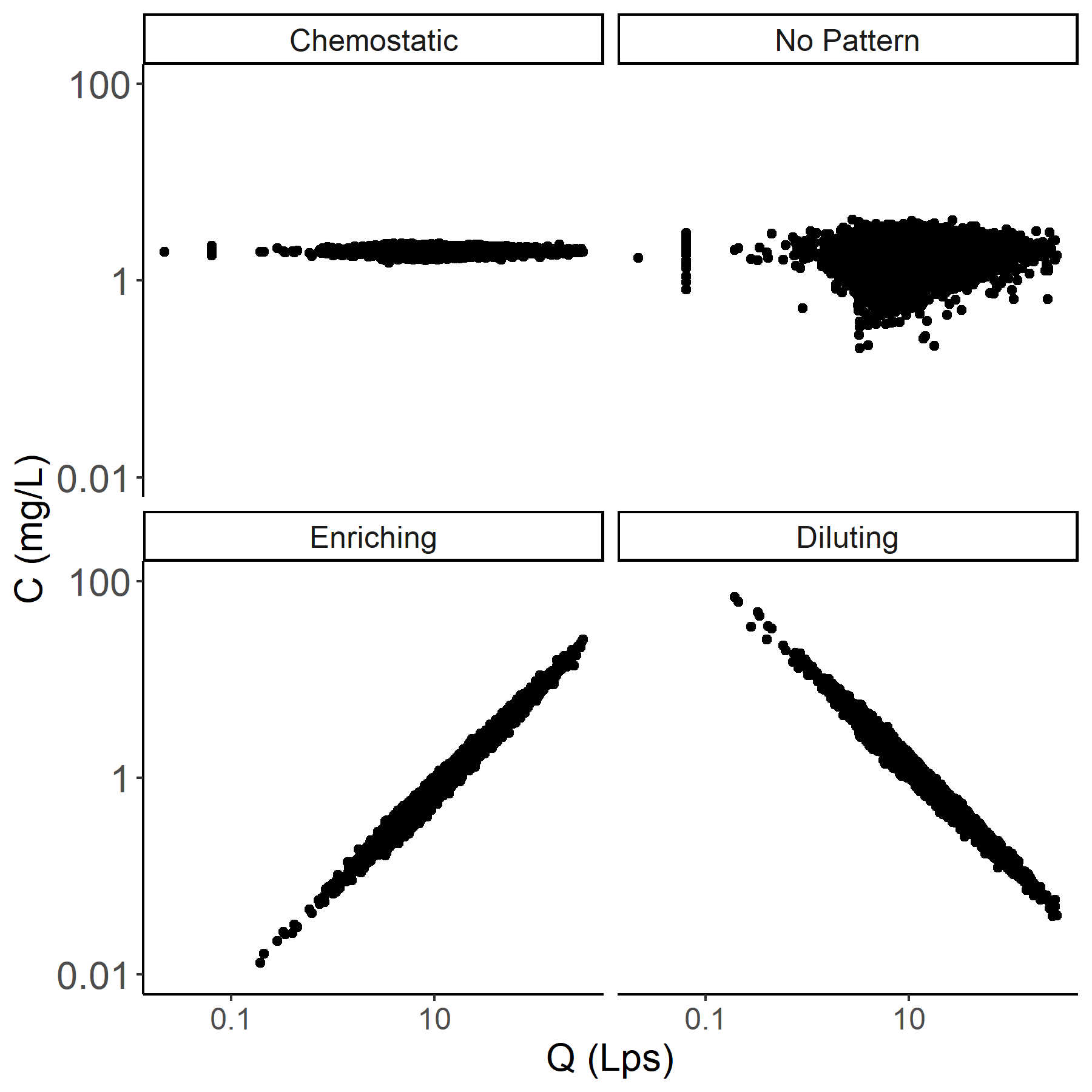


Figure 7: An example of the C:Q regimes created using synthetic hydrology data. Each hydrology time series from the previous section was used to create four concentration time series. The resulting C:Q relationships from applying our methods to one run of the unaltered, modeled time series is represented here.

To assess method accuracy, we calculated ‘true’ flux for each synthetic solute year using the full synthetic time series and the composite method (as recommended in Aulenbach et al 2016) to estimate over less than complete days. The composite method is ideal for this, as the high density of the data yields highly autocorrelated residuals (Aulenbach et al, 2016). We coarsened each synthetic time series of concentration and discharge to the weekly, biweekly, and monthly time steps. Then, we applied each of our four flux methods to each coarsened time series and compared the generated estimates to our true annual flux.

## Generating Estimates for 169 Watershed Ecosystem Studies.

MacroSheds is a synthesis dataset of long-term biogeochemical, hydroclimatic, and geospatial data from small watershed ecosystem studies. The full dataset is available to the public at macrosheds.org. The dataset includes harmonized data from 169 federally funded watershed studies from across the United States (Vlah et al, 2023). To provide flux estimates to the broader community, we applied all four of our flux estimation methods, along with a simple average, as described in Aulenbach et al 2016, to the MacroSheds dataset. Methods were applied individually to solutes at the site-year level. A simplified application of the Aulenbach et al 2016 decision framework was applied to each site-year to give a recommended method. Our method fit a log-log linear model between concentration and discharge for the solute year. We then calculated the autocorrelation of concentration values, the R-squared value of the model and the autocorrelation of the model residuals. Next, we sorted each solute year using a cutoff of 0.30 for the model R-squared. Years with a model R-squared greater than or equal to 0.30 were designated as having ‘strong to moderate’ fits, while years with R-squared lower than 0.30 were designated as having ‘weak to nonexistent’ fits. Solute years with a ‘strong to moderate’ fit and autocorrelated residuals (>=0.20) are recommended to use the composite method, and those without or with weak autocorrelation (<0.20) were recommended to use the rating method. Solute years with a ‘weak to nonexistent’ concentration-discharge fits and autocorrelated concentrations (>=0.20) were recommended to use linear interpolation, while those without or with weak autocorrelation of concentrations (<0.20) were recommended to use a simple average. Only sites with 85% or more days of discharge coverage and at least one chemistry sample per water year quarter were used to calculate loads.

# Results

## Method Sensitivity to Actual High Frequency Data

Results from the data coarsening experiments are represented in figures 8 and 9. Generally, all methods struggled to accurately estimate nitrate load as data become increasingly coarse.

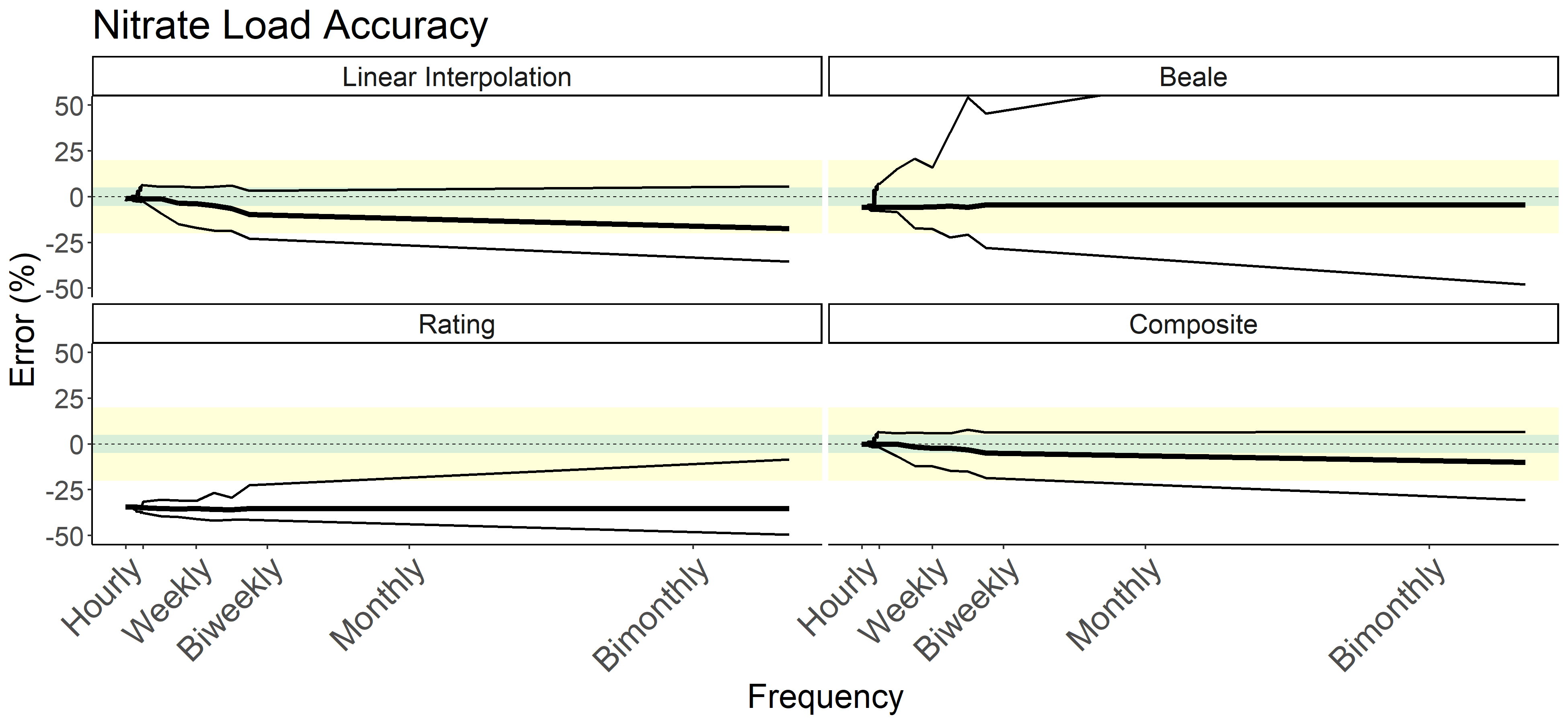


Figure 8: Results from applying four different load estimation methods to artificially coarsened, high-frequency sensor time series of nitrate taken from Hubbard Brook watershed 3. Percent error of estimated annual load from the ‘true’ load, calculated using the full time series, is on the y-axis. Coarsened data frequency is on the x-axis. The solid line indicates the median error for that frequency, with thin lines indicating minimum and maximum. Error within 5% of truth is shaded in green and with 20% in yellow. Note that the linear interpolation and composite methods perform relatively the best for this year of data. However, all methods performed poorly with less than daily data.

Overall, the composite method performed best for this solute year, with accurate median estimates and a relatively low range of potential estimates. Linear interpolation performed comparably with sub-weekly data. When data frequency is high, both concentrations and and model residuals are highly autocorrelated. As expected, under these conditions, methods that leverage these autocorrelations, such as linear interpolation and composite methods, outperform all others. As sampling becomes more infrequent and the autocorrelation of concentrations breaks down, linear interpolation becomes less accurate than the composite method. This is contrary to the guidelines suggested by Aulenbach et al 2016, which - based on the low (~0.07) R-squared of the model fit - would recommend linear interpolation or averaging. Looking at the concentration-discharge relationship presented in figure 4, we see that while the fit is poor, there is still an informative, enriching pattern that the composite method leverages for more accurate interpolation than simple linear interpolation. While relying on the fit alone (the rating method) produces uniformly poor results, including residual corrections greatly improves model performance. It should be noted that the Aulenbach et al 2016 selection method does still select a defensible method (linear interpolation or averaging, depending on sampling frequency), without the benefit referring to the high-frequency time series.

There was a tight relationship between Ca and specific conductance at watershed 3 during the 2016 water year. The fitted linear model had an r-squared of 0.92 and a slope of 0.0063. The error resulting from each method over each coarsening interval is shown in figure 9.

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Figure 9: Results from applying four different load estimation methods to artificially coarsened, high-frequency sensor time series of calcium taken from Hubbard Brook watershed 3. Percent error of estimated annual load from the ‘true’ load, calculated using the full time series, is on the y-axis. Coarsened data frequency is on the x-axis. The solid line indicates the median error for that frequency, with thin lines indicating minimum and maximum. Error within 5% of truth is shaded in green and within 20% in yellow. Note that the linear interpolation generally performs best for this year of data. All methods, excluding the rating method, provided good quality estimates with weekly or finer data frequency.

Generally, linear interpolation performed best for this solute year, regardless of sampling frequency. This is again contrary to what the Aulenbach et al 2016 method would suggest, which - based on the strong (~0.79) R-squared of the model fit - would suggest the rating or composite method. Again, referring to the concentration-discharge relationship from figure 4, we see that there is an enriching trend at high flows that is not captured in our simple model. This is likely what drives the underprediction shown in the composite method results. The range of estimates produced by the rating and composite methods was higher across coarse sampling frequencies than from linear interpolation. As with the NO3-N results, the Aulenbach et al 2016 suggested method does not concur with our analysis but does select a defensible method.

For both NO3-N and Ca, the Beale ratio estimator produced unbiased median estimates from coarse sampling frequencies at the cost of high estimate variance. Due to the underlying assumption of covariance of discharge variance and concentration variance the method performed more accurately on the Ca time series than the NO3-N time series. Users with coarse data interested primarily in reducing bias, rather than error, should consider using Beale derived estimates.

Comparing the results from NO3-N and Ca across methods, we see that using concentration-discharge model fits is a flawed, but useful tool in method selection. While the NO3-N concentration-discharge fit is weak, it provides a useful trend that improves on simply linearly interpolating points. In contrast, even though the Ca time series has a strong concentration-discharge model fit, the model does not accurately describe the true nature of the relationship, chronically biasing our results low. Both cases illustrate the complexity and difficultly of making method selection choices without the benefit of ‘true’ estimates with which to compare.

## Synthetic Time Series

The results for our synthetic time series experiments are shown in figure 10. Fluxes of chemostatic solutes were universally the easiest to predict. Generally, solutes with no obvious relationship to discharge were the most difficult to predict, regardless of method. All methods degraded with increasingly coarsened data. A full table of the results from figure 10 are available in supplementary\_table\_1.csv.

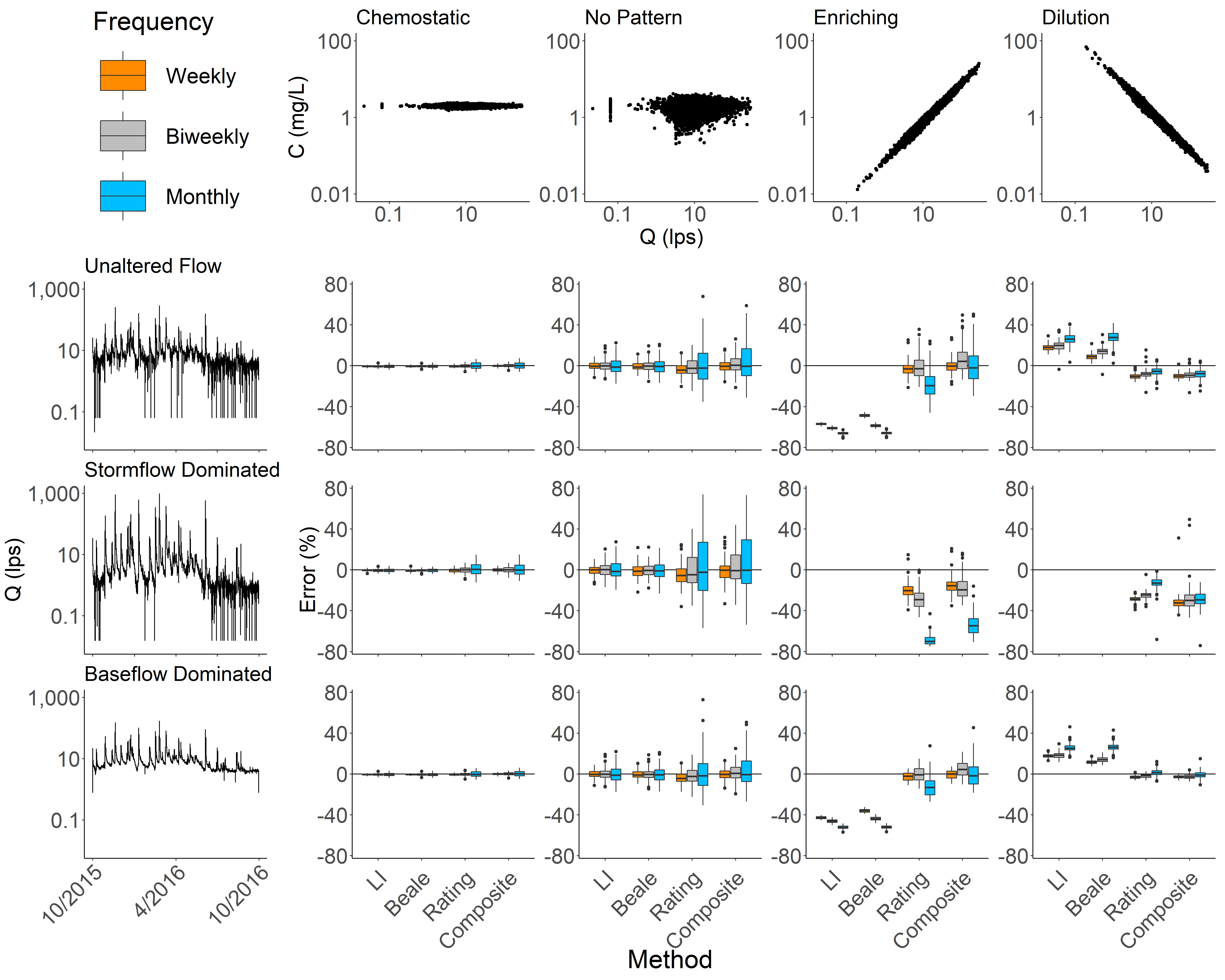


Figure 10: Results from the synthetic time series experiments. The top row of plots describes the concentration discharge relationship. The side column of plots describes the hydrologic regime. The grid of boxplots is the result of applying the four estimation methods across each combination of concentration discharge relationship and hydrologic regime. Linear interpolation (LI) and Beale estimates from enriching or diluting time series under stormflow conditions, and some outlier values (beyond 1.5 interquartile ranges) excluded for readability. A table of summary values for all methods, hydrologic regimes, and C:Q relationships is available in supplementary\_table\_1.csv. Note that no-pattern consistently shows high error, while chemostatic (generally) and enriching (with composite method and high data frequency) give low error.

## Application to Macrosheds Dataset

Applying our methods to the Macrosheds dataset generated 16,489 site-years of data across 93 sites and 112 solutes. Distributions of annual solute loads of nitrate (as nitrogen) and calcium are shown in figure 11. The complete load calculations from each solute and site-year of Macrosheds data are available at https://portal.edirepository.org/nis/mapbrowse?scope=edi%26identifier=1262 , and the latest dataset is available at macrosheds.org.

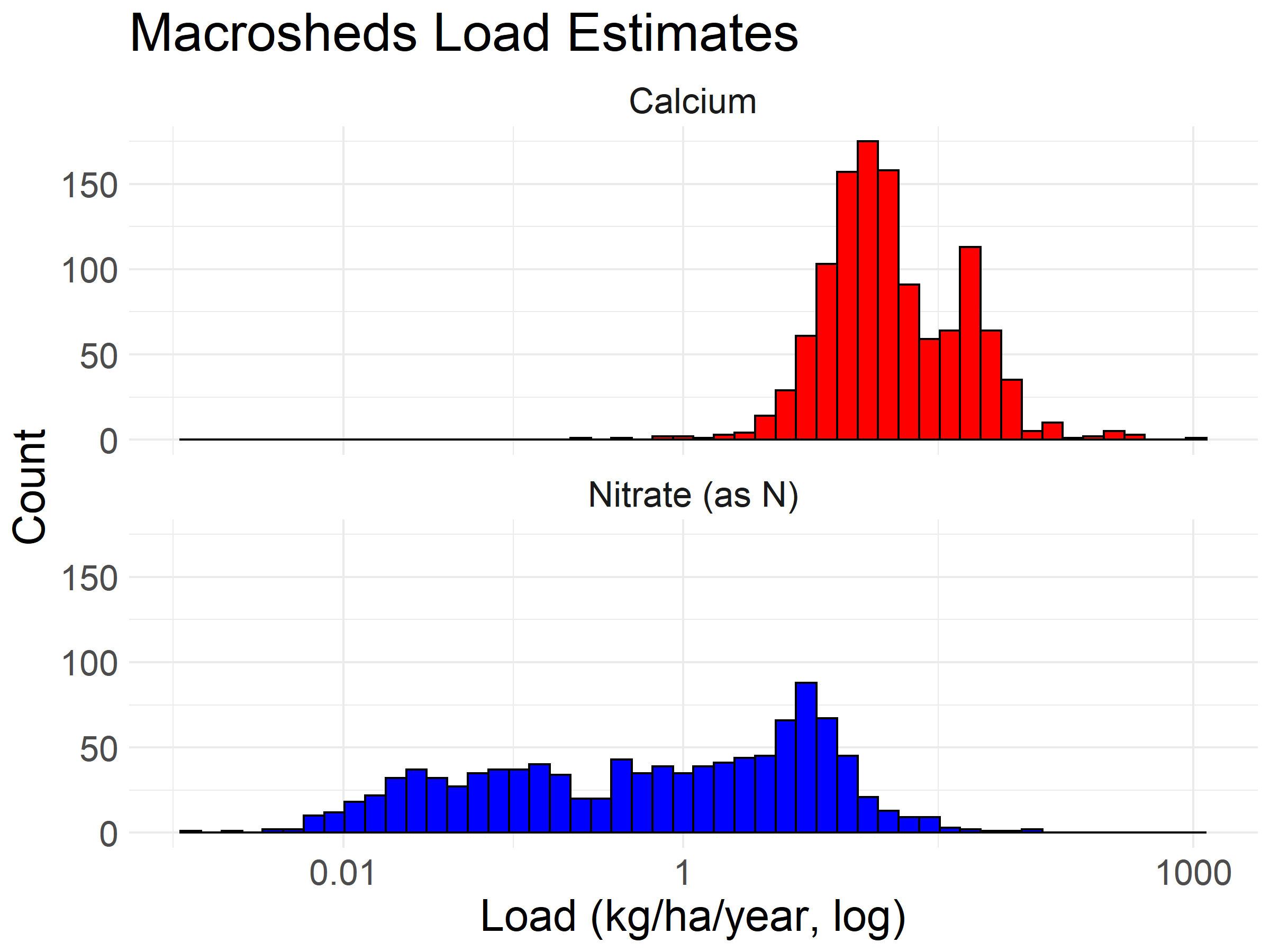


Figure 11: A histogram of annual load estimates present in the MacroSheds dataset. The complete load calculations from each solute and site-year of Macrosheds data are available at https://portal.edirepository.org/nis/mapbrowse?scope=edi%26identifier=1262, and the latest dataset is available at macrosheds.org.

# Discussion

## Insights on Load Estimation Uncertainty

Our results from both sets of experiments generally confirm what Aulenbach and others (2016) observed in their assessment of load estimation methods in small watersheds. Using our simplified application of Aulenbach and others’ (2016) method selection procedure yields a defensible selection of load estimation methods. As shown in figure 12, other single methods also provide reasonable estimates. However, it would be difficult to confidently assess their relative effectiveness without a sensor derived ‘truth’ for comparison.

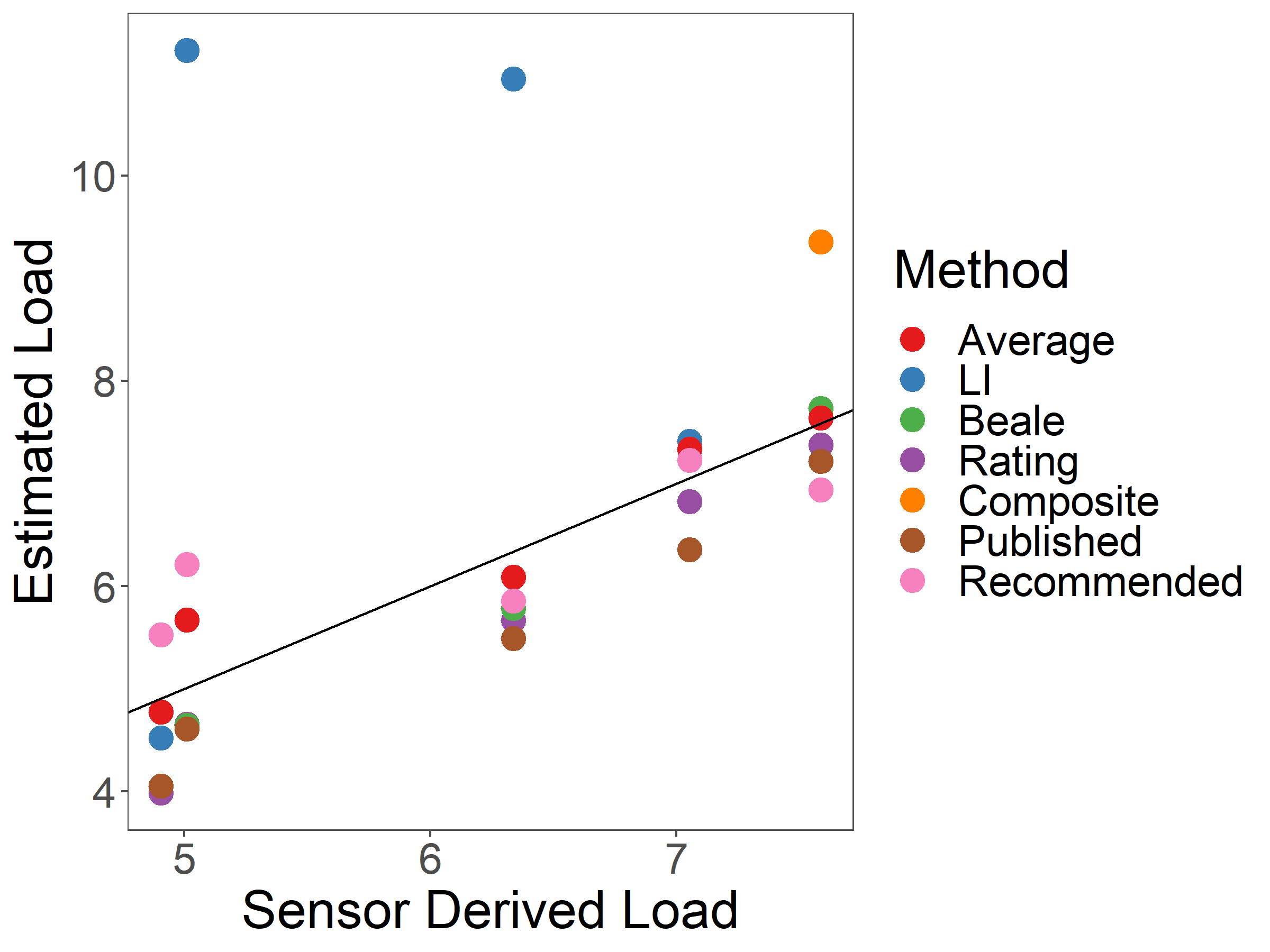


Figure 12: A comparison between load estimation methods made with data from watershed 3 at Hubbard Brook Experimental Forest. Sensor derived load is calculated using 15-minute specific conductance data, converted to calcium concentrations via regression, with the composite method applied. Estimated loads were calculated using biweekly, discrete grab samples. Values published from Hubbard Brook are in brown. The estimate recommended by our simplified application of Aulenbach et al 2016 is in pink. A 1:1 line is plotted in black.

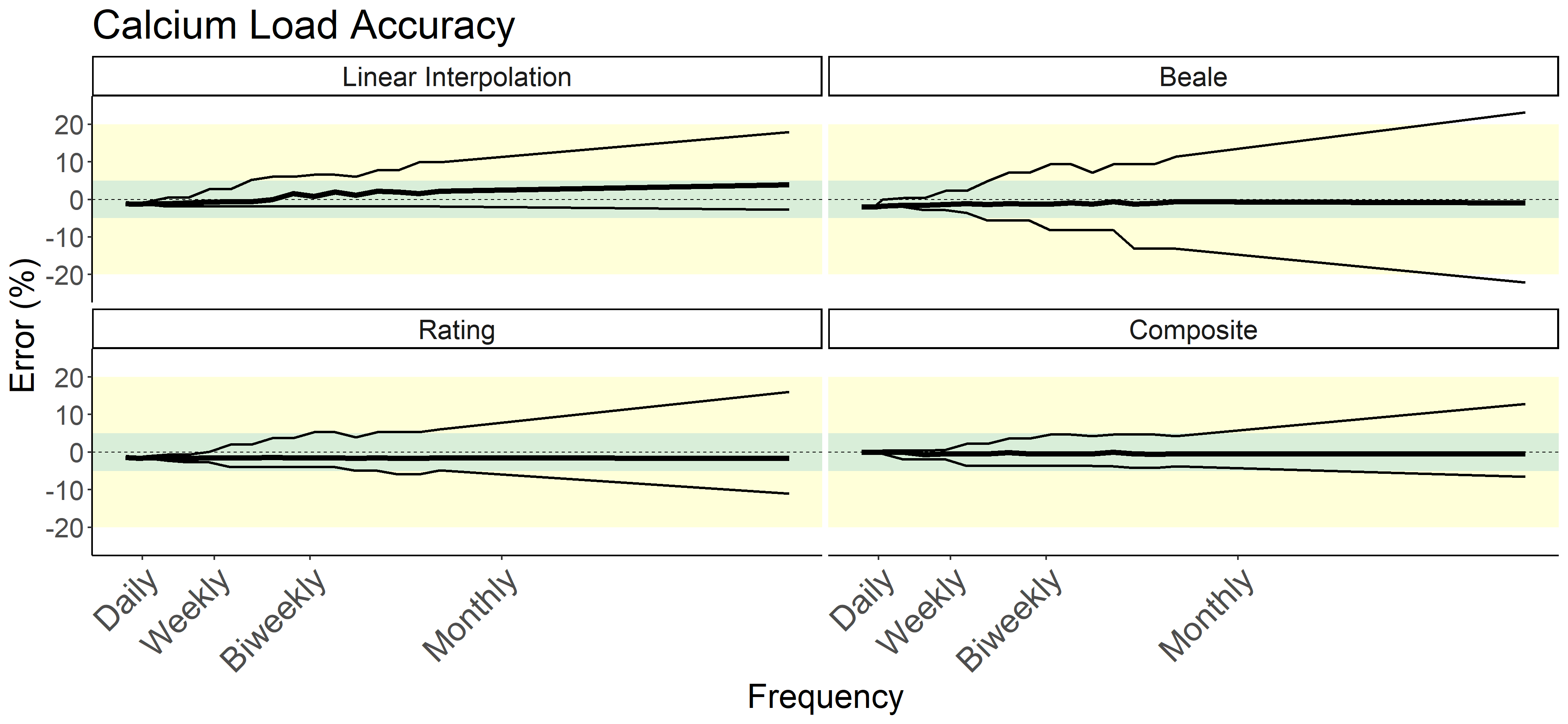
The results in figure 12 are a reaffirming case study that the Aulenbach 2016 decision flowchart sensibly chooses from among the best load estimation methods, without requiring the use of outside data.

Our results also reinforce previous findings that – generally - when there is not a strong concentration-discharge relationship, users should rely on linear interpolation or averaging methods. This is evident in figure 10 under chemostatic or no-pattern concentration-discharge relationships. Under these chemodynamics, linear interpolation and the Beale estimator outperform the rating and composite methods, regardless of hydrologic regime. Consider a load estimate from a solute with no underlying concentration-discharge pattern, stormflow dominated hydrology, and monthly sampling. Our experiment shows linear interpolation yields a mean error of -0.43% (95% confidence interval of -19.11% to 18.25%). Meanwhile, the composite method yields a mean error of 8.44% (95% confidence interval of -55.67% to 72.55%).

When there is a strong concentration-discharge relationship, researchers should use a method that leverages that relationship. Our results in figure 10 confirm that when the concentration-discharge relationship is stable and effectively modeled, concentration-discharge informed methods tend to outperform others. Under such conditions, the rating and composite methods dramatically outperform linear interpolation or the Beale ratio estimator. For example, a load estimate from a solute with a diluting concentration-discharge relationship, stormflow dominated hydrology, and monthly sampling has a mean error of -13.43% (95% confidence interval of –27.44% to 0.58%), while linear interpolation yields a mean error of 119.57% (95% confidence interval of 85.47% to 153.67%).

Results from the data coarsening experiment give nuance to the synthetic time series experiments. Methods applied less cleanly to the concentration-discharge relationship in the coarsened Ca time series (figure 9) than in our synthetic time series testing. The concentration-discharge relationship present in the calcium time series (figure 4) gives a high R-squared of 0.79 and a low slope of -0.12. While it produces low mean error, linear interpolation (the best available method) still produces estimates that can overpredict load by as much as 11% at monthly sampling frequencies (figure 9). Our synthetic time series experiment expected much smaller error given the conditions, with maximum error of 3.34%. This shows a limitation of our synthetic time series analysis; the variance of the underlying time series (both in streamflow and chemistry) has a scaling effect on uncertainty. The calcium time series has a standard deviation of 0.23 mg/L, while the synthetic, chemostatic time series has a standard deviation of 0.1 mg/L.

This effect is further illustrated when we apply our coarsening experiment to data from the 2008 water year at Upper Hafren site of the Plynlimon research catchments (Kirchner and Reynolds, 2013). This dataset contains hydrochemistry data taken every 7 hours from a small stream in Wales, UK. Compared to watershed 3 at Hubbard Brook, the Plynlimon dataset has much less variable stream chemistry. For the 2008 water year, there was a mean nitrate (as nitrogen) concentration of 0.14 mg/L with a standard deviation of 0.06 mg/L and a mean calcium concentration of 0.51 mg/L with a standard deviation of 0.11 mg/L. As shown in figure 13, this lower variance yielded more precise estimates across all methods.



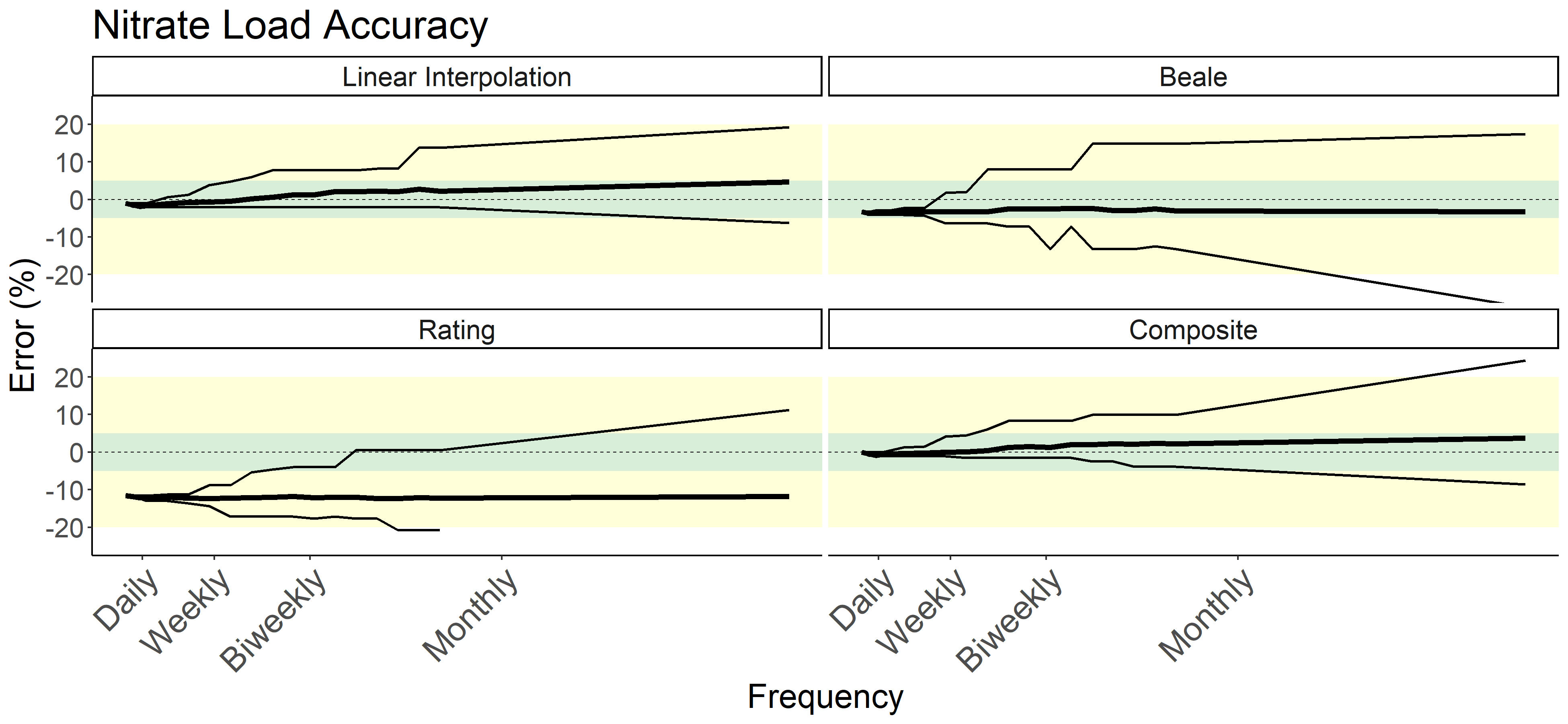


Figure 13: Results from applying four different load estimation methods to artificially coarsened, high-frequency sampling time series taken at Plynlimon Research Catchment. Percent error of estimated annual load from the ‘true’ load, calculated using the full time series, is on the y-axis. Coarsened data frequency is on the x-axis. The solid line indicates the median error for that frequency, with dashed lines indicating minimum and maximum. Error within 5% of truth is shaded in green and with 20% in yellow.

Considering the results of the synthetic time series and comparing our HBEF case study to Pylimon highlights an important conclusion for macroscale scientists interested in load estimation: if variance in solute chemistry is sufficiently low, knowing water flux is enough to accurately estimate solute loads. However, doing so with confidence requires high-frequency data or an explanatory, well-defined C:Q relationship.

## Challenges for Macroscale Science with Load Estimates

The results of our efforts highlight serval important challenges for scientists working with load estimates.

Firstly, method selection is deeply important for accurate load estimation. The results of our data coarsening experiment (figures 8 and 9) clearly show that–especially at coarse sampling intervals–method selection greatly influences the potential range of estimates generated. When a load estimate is provided without documentation of the underlying methodology, it should not be trusted. Researchers interested in cross site comparisons are better served by using the underlying chemistry and discharge time series to recompute undocumented load estimates using known methods. The work necessary to do so can be eased using tools like the ‘RiverLoad’ and ‘Macrosheds’ R packages.

Additionally, our experiments give substantial evidence that at sampling frequencies commonly used in ecosystem studies (in the range of weekly to bimonthly) non-chemostatic load estimates should be used with careful consideration, especially in stormflow dominated sites. While the appropriate method at a weekly sampling frequency would often produce a low mean error, the extent of possible error observed over 100 runs was still problematic. For example, under a stormflow dominated hydrologic regime, with no concentration-discharge relationship, and weekly sampling, linear interpolation (the best performing method) gave a mean error of -0.2%, but the 95% confidence interval spanned from -10.59% to 10.92.

Finally, knowing fit of the concentration-discharge relationship alone is not enough to assign confidence to underlying load estimates generated from that solute time series. Users need to first assess how high their confidence is in knowing the entirety of the concentration-discharge relationship. A site that biases its collection towards baseflow days (which is common with non-event supplemented sampling) may erroneously conclude that their enriching solute’s concentration-discharge relationship is chemostatic or has no pattern. A user making this conclusion would be tempted to use linear interpolation or the Beale ratio estimator to reduce both error and bias. This yield load estimates that heavily underestimate true load for the year. The importance of a well defined concentration-discharge relationship is also evident when considering the effect of diluting conditions in figure 10. Moving from weekly to monthly sampling frequencies counterintuitively decreases bias, while increasing the range of possible errors. This is likely due to an overfitting of the rating model to baseflow points decreasing rating accuracy at low flows. Results from the data coarsening experiments suggest this trend would reverse at high sampling frequencies. We see a similar effect in the enriching time series, where biweekly sampling shows less bias than weekly sampling. These data suggest that simply ‘fitting and forgetting’ a rating model is not enough to generate the best possible load estimates.

Put simply, truly assessing confidence in a load estimate requires an assessment of confidence in both the concentration-discharge relationship itself and an assessment of confidence in having the entire concentration-discharge relationship. All the challenges delineated here point to a clear need for more long-term, high-frequency records of stream chemistry. While it may be eventually possible to estimate loads accurately from sparse records using machine learning or other emerging computing methods, currently there is no substitute for high quality, frequent observations.

## A Framework for Considering Load Estimates

The challenges from the previous section are easy to identify, but difficult to solve, especially for scientists interested in cross-site comparisons. While other researchers can rely on an intimate understanding of the history and disturbances at each site to inform their confidence in estimates, macroscale scientists must rely only on the data provided from previous studies. Important site history narratives and key assumptions may be difficult to locate in publications and metadata, if they are recorded at all. Cultivating a rich and well-informed understanding of every individual site is often not feasible, and depending on publicly accessible documentation, may be impossible. However, excluding good data from a synthesis effort is wasteful and limits the power of analyses and the scope at which synthesis can be performed. Therefore, it is necessary to develop a framework of assessing load estimate confidence using only the site records themselves.

We propose the framework presented in figure 14. As C:Q relationships have been shown to change over time (Kirchner et al, 2004; Godsey et al, 2019) and this framework is built on the assumption that the user does not have intimate site knowledge, each site-year is assessed independently. Our framework also assumes users have a complete flow record for the site and that they have chosen the most appropriate estimation method for each solute as described in Aulenbach et al 2016.

With effort, this framework could be greatly improved by grouping data and method selection across multiple solute years with known, stable chemodynamics. Doing so would leverage the power of long-term data and allow for much more well-informed concentration-discharge models - generating higher confidence estimates. However, doing so requires the user to have a reliable method to assess the stability of concentration-discharge relationships within individual solutes and to develop methods to handle transitions between regimes. Currently, the authors are not aware of any such methods or tools.

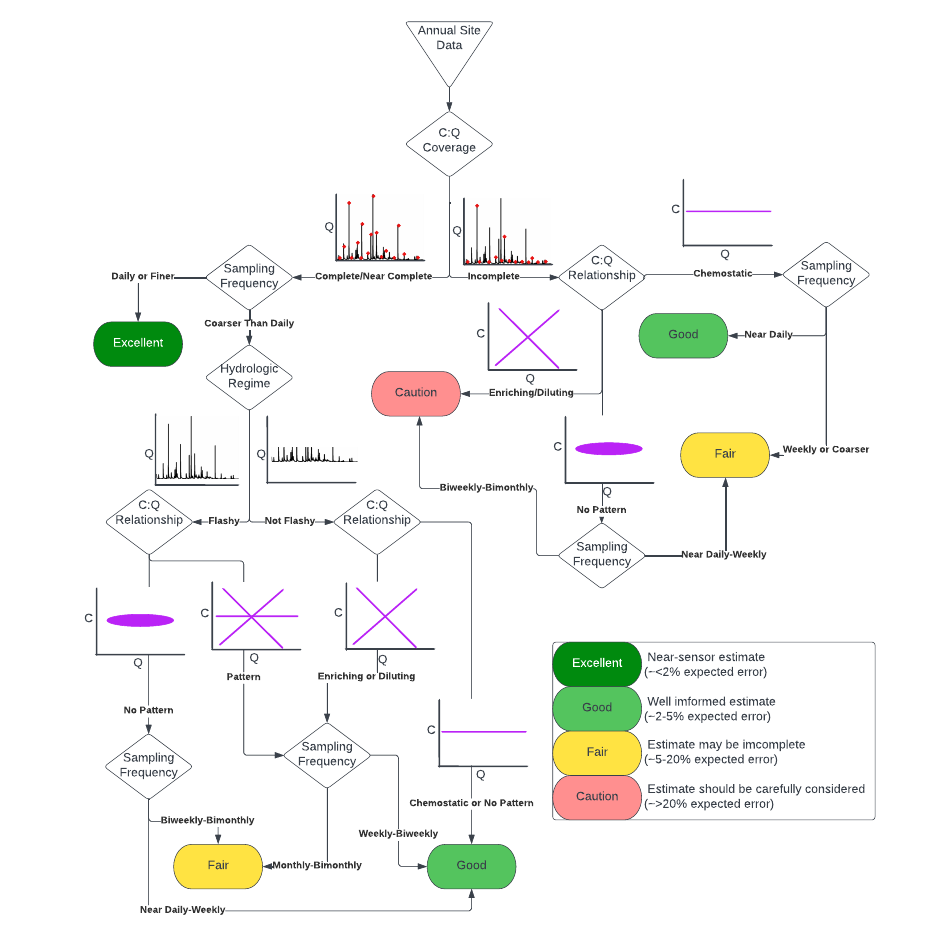


Figure 14: A conceptual flowchart for classifying confidence in load estimates, assuming a complete discharge time series and method selection as described in Aulenbach et al 2016. C:Q coverage refers how completely the extent of the C:Q relationship has been confirmed for the given site-year. Sampling frequency is the rate at which chemistry is sampled at the site. Hydrologic regime is either defined as flashy (stormflow dominated) or not flashy (baseflow dominated). Site-years with total C:Q coverage and high sampling frequency produce ‘excellent’ estimates. Non-chemostatic site-years with incomplete C:Q coverage produce ‘fair’ estimates or estimates that should be treated with ‘caution’.

Data binned as ‘excellent’ or ‘good’ is likely suitable for inter-site comparisons at large scales. Data binned as ‘fair’ should only be used for limited applications. For example, ‘fair’ rated estimates could be used in aggregated regional estimates of weathering rates. Data binned as ‘caution’ should not be used without the user learning more about the site. It is possible that ‘caution’ rated estimates have lower error than expected, especially if the site they are derived from has been long-running and uses targeted sampling. It should be noted that while error ranges are presented for each category, they are a qualitative assessment guided by the results of our experiments. Further work will be required to truly constrain expected error for such a complex problem.

While it is beyond the scope of this effort to delineate exact boundaries for each branch in figure 14, we fully expect to be able to do so robustly as more sensor data becomes available in a variety of small watershed systems. With adequate, widely distributed sensor data, we expect the factors identified in our framework could be used to sort load estimates by relative quality. Concentration-discharge coverage can be systematically assessed by creating a ratio of sampled flows to observed flows over the year. Sampling frequency can be easily evaluated from the stream chemistry record. The shape of the concentration-discharge relationship can be determined by fitting a log-log simple linear model between solute concentrations and discharge at the site and assessing the slope, R-squared, and residuals of the resulting fit. Chemostatic and no pattern time series could be differentiated using a ratio of concentration time series’ standard deviation to its mean. Hydrologic regime can be assessed using the Richards-Baker flashiness index (Baker et al, 2004) or using the baseflow-quickflow separation method used in this study. While the field gathers more sensor data, we encourage the larger macroscale watershed science community to continue to test and model the effects of these variables on load estimation.

We hope the framework provided here can unlock macroscale science efforts that rely on load estimates and empower synthesis scientists to delve into the rich library of datasets available to them from past studies.

# Supplement

Supplemental Table 1: A table of the results from the synthetic time series experiments. All values (except for number of outliers, which is a count) are expressed in percent error.

(supplemental table 1 is available as supplemental\_table\_1.csv)